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Fatigue lifetime of a RC bridge along the Carajás railroad

Vida útil à fadiga de uma ponte ferroviária na estrada de ferro Carajás



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Abstract

The aim of this paper is to present and discuss the results obtained with a methodology used to characterize the concrete and to evaluate the structural safety against fatigue of the reinforced concrete bridge number 50A located in the Carajás railroad. An "in situ" inspection was carried out in order to assess the evolution of damage in structural elements, with reference to information available in existing projects, calculation memory and reporting of previous inspections. Extractions of concrete testimonies, alkalinity tests, sclerometry, pacometry and laboratory tests were also performed to characterize the materials mechanically and estimate the structural behavior of the bridge under higher future loads.

Keywords: bridge, structural monitoring, reinforced concrete.

Resumo

O foco principal deste trabalho é apresentar e discutir os resultados obtidos com a metodologia utilizada para caracterização mecânica do concreto e avaliação da segurança estrutural à fadiga da ponte número 50A, em concreto armado, localizada na estrada de ferro Carajás. Foi realizada uma inspeção "in loco" com o objetivo de avaliar a evolução dos danos nos elementos estruturais, usando como referência informações disponibilizadas em projetos existentes, memorial descritivo de cálculo e relatórios de inspeções anteriores. Foram realizadas extrações de testemunhos, ensaios de alcalinidade, esclerometria, pacometria e ensaios laboratoriais que permitiram caracterizar mecanicamente os materiais e estimar o comportamento estrutural da obra de arte sob carregamentos futuros maiores.

Palavras-chave: ponte, monitoramento estrutural, concreto armado.

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1. Introduction

The bridge over the river Mãe Maria is located in the city of Marabá, Pará state, and is part of the Carajás Railroad (EFC). It is used to allow iron ore transport from Carajás, a city in Pará yet, to Itaqui harbor in São Luis city, state of Maranhão. Due to the need for load increasing, which currently is 320 kN to 400 kN per axle, studies focused on the new behavior of the structure are of extreme importance for the service life of this bridge.

1.1 Structural system description

The studied bridge is a straight line structure located along the Carajás Railroad crossing the river Mãe Maria, identified as OAE 50A. Built in reinforced concrete, cast "in situ", the OAE has two hyperstatic spans, totaling 64.20m, crossing the bed of the river with two spans of 20.00 m providing a cross section width of 5.85

m. On the deck slab is the rail line superstructure for passage of trains. Safety on the OAE is guaranteed with the presence of refuges and metal railings as shown in Figure 1.

The superstructure is slab on beams type. The deck consists of four spans of continuous stringers of "pi" cross section, with linear variation of the web thickness from 0.35mto 0.70 m near the supports and block B2, as shown in Figure 2, stiffened by transversal beams (secondary) on charted neoprene support devices at the abutmentE1 and block B2. The beams are embedded in the abutment E2.



Figure 3 shows the overall structural system with beams, abutments, blocks and reinforced concrete caissons cast "in situ".

1.2 Dynamic loads

The fleet of locomotives and wagons currently in operation for transporting ore in the EFC is composed mostly of locomotives DASH9 which represents almost 30% of the total fleet, as shown in Table 1, and GDT wagons that represent about90% of the fleet. Basically two types of compositions are applied, being one composed by two front locomotives followed by 104 wagons, plus one intermediate locomotive and more 104 wagons, which corresponds to 80% of the fleet in operation. There are situations where the position of the intermediate locomotive varies and may stay at the end of the composition. The other composition uses three front locomotives pulling 208 wagons. Figure 4 shows the longitudinal distances considered for locomotives and wagons.

In the future, the EFC will be loaded by new trains-types, with a greater number of wagons and individual load higher than the present. It is intended to work with two models, where the basic difference is the number of locomotives between the wagons. In the first situation there are 2 locomotives + 110 wagons + 1 locomotive + 110 wagons + 1 locomotive + 110 wagons. On the second, the configuration is 2 locomotives +110 wagons + 2 locomotives + 220 wagons. Table 2 shows the loads for the current and future operational trains-types considering GDT wagons and DASH9 locomotives.

Figure 2 - (a) bridge's cross section (meters); (b) linear variation of the stringers' width close to supports







1.3 Documents analysis and preliminary inspection

To evaluate the current state of the structure is necessary to consider a set of actions which bring together enough information. This information set came from a data analysis and reports already made by specialized companies, along with visual inspections of the bridge. Were consulted documents related to existing projects, descriptive history calculation and reports that describe changes in pathological conditions, as well as the preventive measures taken, and a preliminary qualitative evaluation of the current state of the bridge was done. It was found that the structure is in accordance



with the geometric and structural information from the projective documents.

In relation to the visual inspection of the stringers and crossbeams were observed discrete increases in lengths of the cracks in the stringers, when compared with those shown in the cracking maps shown in previous reports. Although agreeing with Cánovas [1]

Table 1 - Operational locomotives and wagons details (Source: Vale)							
	Locomotives technical characteristics - EFC Situation in April/2007						
Fleet	Model	Total Pot. (HP)	Liq. Pot. (HP)	Engine	Amt.	Manuf. year	
GE	C36-7B (DASH-7)	3.600	3.600	7FDL16G60	39	1984/1987	
GE	C40(DASH-8)	4.000	4.000	7FDL16K10	4	1989	
GE	C44CW (DASH-9)	4.400	4.374	7FDL16n50	55	1997/2001	
GE	C-SL65	600	600	NTA855	1	1993	
GM	SD40-2	3.000	3.000	16-645 E3C	27	1984/1987	
GM	SD60M	3.800	3.800	16-710 G3A	2	1992	
GM	SD70M	4.300	4.300	16-710 G3C	55	2001	
	Locomotive fleet in operation: 183						

Table 2 – Loads from operational and future train type					
Situation	Locomotive DASH9	Loaded GDT wagon	Unloaded GDT wagon		
Current	300 kN/axis (1800 kN)	325 kN/axis (1300 kN)	52,5 kN/axis (210 kN)		
Future	300 kN/axis (1800 kN)	400 kN/axis (1600 kN)	52,5 kN/axis (210 kN)		

Figure 5 – Support (block) and instrumentation of the stringer



that the progression of cracking is an indication of symptomatic occurrence of a defect, it is believed that in this case, the cracks are the result of shrinkage of the concrete at early ages and that the differences could be related to the methodologies of measurement of these lengths. Efflorescence due to the dissolution of the compounds of the cement paste were also observed, according to Cascudo [2], infiltration, surface segregation and insufficient reinforcement coatings in concrete beams. On the crossbeams were also observed efflorescence and moisture stains. Generally, the stringers and crossbeams have satisfactory integrity, as shown in Figure 5.

During the inspection of the deck a heavy cracking pattern with efflorescence was noticed. On the stringers the presence of short or damaged drains led to the occurrence of moisture stains. Already on the side cantilevers were observed cracks with and without efflorescence and infiltration, as shown in Figure 6. In the transition slab were not observed gaps, being therefore in satisfactory conditions. The design of the structure according to the available information in the calculation history was performed using the compressive strength of concrete corresponding to 18.0 MPa. For the foundations, was admitted concrete with compressive strength of 15.0 MPa and land with admissible stress of 0.8 MPa. The criteria used were based on the NBR 6118 : 1978 [3] to be the design code at the time of preparation of the project.

In this last inspection were inspected areas of the upper face (0.3 mx 0.3 m), where it was possible to remove the gravel ballast, and bottom face of the deck slab with the aid of a stair, as shown on Figure 7, and the existence of cracks was not verified on these surfaces. In Figure 8, it can be seen that the support devices of the abutment E1 shows no visible abnormalities, only natural strains



Figure 7 – Slab concrete surface preparation for instrumentation







Figure 10 - Pacometry testing on stringer

due to usage and dirt. Other support devices are under similar conditions to the support device of the abutment E1, but still suitable for use.

2. Concrete characterization

2.1 Non-destructive tests

Non-destructive tests (NDT) include various methods of analysis of materials, components and connections in order to identify and quantify internal defects and degradations. The NDT main goal is to enable evaluation of the materials properties before any failure occurs, basing such evaluation on recognized criteria for acceptance or degradation profiles defined over years of experience, so that the quality and performance of these materials in service are ensured. This has generated a growing interest in developing methods for non-destructive testing for concrete structures evaluation, according to Mehta [4].

The pacometry test was performed before the sclerometry tests to determine the position of steel bars for both the sclerometry tests and for instrumentation of the reinforcements with strain gages (EER). In this investigation a pacometer was used and its operating principle is electromagnetic, to determine the presence and direction of the bars, as well as to determine the thickness of the concrete coatings in relation to the external surface of the bars. Figure 9 shows the pacometry testing on caisson T7 and, in Figure 10, on a stringer. The spacing between bars varied from 0.05 m to 0.11 m. Pacometry tests were also carried out on the deck slab for steel bars detection to avoid damage during the testimony extractions.

The sclerometry tests were performed on all structural elements of the bridge. This method basically consists in evaluating the superficial hardness of the hardened concrete using a device which measures the energy of impact on the reflection surface. The method known as "rebound hammer method" provides an index (denominated sclerometric index) having direct correlation with the compressive strength of concrete. However, there are several





Figure 11 - Sclerometry testing on slab (left) and stringer (right)



studies that point to other factors that affect these correlations outlined by the calibration curves. According to Evangelista [5] factors as the amount of cement, aggregate nature, maturity and moisture content, carbonation and surface finish, can increased propagation of errors in the results. The concrete strength was estimated based on the arithmetic average of the resistances of nine points of each study area (0.10 mx 0.10 m), according to NBR 7584 : 1995 [6]. Figure 11 shows the application of sclerometer and arrangement of the points on the deck slab and stringer.

2.2 Destructive tests

Tests for determining the depth of carbonation in structural el-



ements of the OAE using a solution with the chemical indicator phenolphthalein were performed "in situ". After opening of the windows in 0.05 m thick concrete coating, the tests were conducted in various structural elements and showed that the concrete is at a satisfactory level of alkalinity, with no visible sign of corrosion. Figure 12 shows the final appearance of the concrete after the alkalinity testing (pink color indicates the





Figure 14 - Testimony's length standardization and end surface regularization

alkaline concrete with no carbonation).

To determine the mechanical properties of concrete testimony were extracted from the structural elements by using a cutting machine with rotary diamond crown shown in Figure 13. A total of five concrete testimonies, two from the abutments, two from the slab and two beam from the stringer. The testimonies that had flaws in their end faces, due to the extraction process were rectified with the aid of a circular saw, resulting in a final length of 200 mm, as shown in Figure 14. Regarding the tests to determine the modulus of elasticity and compressive strength of concrete, the testimonies were tested following the recommendations of NBR 8522 : 2003 [7] and NBR 5739 : 1994 [8], where

the first recommended to be realized three cycles of loading and unloading with peaks corresponding to 30% of the failure stress (fc) and 0.5 MPa . For this a servo-controlled machine model PC-200CS, manufacturer EMIC, was used. Tests were then performed with constant load speed rate of 0.25 MPa/s. After the cycles of loading and unloading, a loading was applied progressively until failure by crushing of the testimony. In addition to the strain sensor type "clip gauge", still from the manufacturer EMIC, two strain gages acquired from the company Excel Sensors Ltd., Model PA-06-201BA-120L, were installed at half height of the testimony and diametrically opposed. Figure 15 shows details of the tests in the laboratory.



Table 3 – Compressive strength of concrete from sclerometry tests							
Impact	Compressive strength f _c (MPa)						
	Stringer	Slab	Block	Abutment 1	Abutment 2	Caisson T7	
1	60	61	52	56	60	43	
2	52	61	48	46	58	46	
3	42	61	52	59	59	43	
4	54	60	55	60	62	42	
5	62	65	54	60	62	47	
6	62	61	52	58	62	37	
7	56	63	56	50	62	45	
8	56	63	54	56	61	42	
9	42	63	54	55	59	42	
Average	54	62	53	54	61	43	

Table 4 – Experimental mechanical properties of concrete					
Testimony	E _c (GPa)	f _c (MPa)			
Abutment 02 (CP01)	38,6	51,5			
Abutment 02 (CP02)	42,4	52,3			
Slab (CP01)	41,1	39,2			
Slab (CP02)	44,0	50,0			
Stringer (CP01)	58,8	38,7			

3. Concrete mechanical characterization results

The Schmidt rebound hammer method is simple to use and offers a quick and cheap way to evaluate the uniformity of the hardened concrete "in situ", so the test result is susceptible to factors such as: concrete mix proportion, age and environmental conditions, surface roughness, moisture condition, surface carbonation, the element stiffness and location of the hammer. The sclerometry average results for the "in situ" studied elements are presented in Table 3.

The results observed with the non-destructive testing of sclerometry were all higher than those for the testimonies. According to Malhotra [9], the accuracy in estimating the strength of











concrete in laboratorial tests, with a properly calibrated rebound hammer is \pm 15% 20%, and in a concrete structure is \pm 25%. The measurements of modulus of elasticity of the concrete (Ec) determined experimentally according to NBR 8522 : 2003 [7], are presented in Table 4 together with the resistance to axial compression experimentally determined in accordance with NBR 5739 : 1994 [8].

In Figures 16 to 20 it can be seen the result of the configuration adopted for the tests as a function of time, where the loads ranged from 0.5 MPa to 30% of the failure stresses estimated for the concrete testimonies according to the current code prescriptions, and the stress-strain diagrams generated as the tests were performed.

Structural project analysis according to codes' prescriptions

4.1 Dead load effects on the stringers

All permanent loads (corresponding to stringers self-weight,

crossbeams, refuges, ballast, rails, accessories, etc.) and dynamic loads were separately considered, corresponding to the several trains type studied (Cooper E80, operational, loaded, future loaded and unloaded operational train-type). Figure 21 shows, respectively, bending moment and shear force diagrams due to permanent loading from the computational program SAP2000 [10].

4.2 Dynamic loads history

For the determination of the applied loading on the stringers (bending moment and shear) each of the spans was subdivided into ten parts, resulting in 21 sections, as done in the calculation memory. As illustration, the forces' variation from SAP200 [10] for section 21 is presented, corresponding to the fix point between the deck slab and abutment E2 and considered the most requested section under several trains types passage without permanent loads. The other sections time histories were also obtained, but only their envelopes are presented. Figures 22 to 25 show the dynamic loading history for several trains.









Table 5 – Results for elasticity modulus of concrete						
Sample	E _c experimental (GPa)	${\sf E}_{\rm c}$ estimated (GPa)		Difference (%)		
	NBR 8522	NBR 6118**	MC90***	NBR6118	MC90	
Abutment 02 (CP01)	38,6	40,2	37,2	4,1	3,6	
Abutment (CP02)	42,5	40,5	37,3	4,7	12,2	
Slab (CP01)	41,0	35,1	33,9	14,3	17,3	
Slab (CP02)	44,0	39,6	36,8	10,0	16,3	
Stringer L.E* (CP01)	58,8	34,9	33,8	40,6	42,5	
* Left side						
** $E_c = 5600 \cdot \sqrt{f_c}$ (MPa)						
*** $E_{a} = 2.15 \cdot 10_{4} \cdot \sqrt[3]{0.1 \cdot f}$ (MPq)						

5. Cross sections' fatigue lifetime

To determine the fatigue lifetime of the stringers was considered, initially, the variation of bending moment due to train operational loaded, future loaded and unloaded. From the variation of bending moment, it is possible to determine the strains and stresses at any point of the cross sections. Figure 26 shows theoretical variations of the strains, respectively, in the concrete and reinforcement of the section S21 due to the passage of the train operational loaded. The coordinates indicated in the legend of the Figure 26a indicate the position (height) of the concrete fiber analyzed in relation to the lower face of the section. According to NBR 6118 : 2003 [11] and Model Code MC90 (CEB-FIP, 1992) [12] should be estimated minimum and maximum stresses in an area not exceeding 300 mm from the edges of the cross section. For this reason, in the figure are shown four curves corresponding to the fibers located 300 mm from the upper and lower edges of the stringer. Since Figure 27 shows respectively the theoretical compression stresses in the concrete and in the reinforcement of the section S21 due to the passage of the train type operational loaded.

For a preliminary check to fatigue of concrete were considered the prescriptions of NBR 6118 : 2003 [11]. According to this standard, checking the fatigue of concrete is ensured if the maximum compressive stress in concrete (corrected for the gradient of compressive stress) does not exceed a limit fatigue stress $f_{cd,fad} = 0.45 f_{cd}$. This check is presented in Figure 28, where the rectified stress is provided in module (with positive sign indicating compression, in this case). Whereas the design compressive strength for the concrete, i.e. $f_{ck} = 18$ MPa and a safety coefficient $\gamma_c = 1.4$, the fatigue limit stress is $f_{cd,fad} = 5.78$ MPa. Thus, according to NBR 6118 : 2003 [11], only the stresses arising from the permanent load would already be very close to this limit in section S21. It should be remarked that this criterion is quite conservative, since it does not consider the stresses variations.

As already mentioned, the section "23.5 Ultimate limit state of fatigue" of NBR 6118 : 2003 [11] is based on the "6.7 Ultimate





Figure 27 – Stringer's stress theoretical variation in section S21 due to passage of the loaded operational train type on concrete (left) and reinforcement

Stress (kN/m²) Stress (kN/m²) x(1)= +0.05m y(1)= +2.76m -3000 0 +0.05m v(2)= +0.05m d(2)= -4000 -0.5 -5000 -1 -6000 L 0 -1.5 1000 2000 500 1000 1500 2000 2500 3000 500 1500 2500 3000 3500 0 3500 Time (s) Time (s)

limit state of fatigue" of Model Code MC90 (CEB-FIP, 1992) [12], which sequentially presents three methods for design verification with increasing levels of refinement and precision. To verify the fatigue of concrete, the NBR 6118 : 2003 [11] brings only the most simple and therefore more conservative method. Moreover, the Model Code MC90 (CEB-FIP, 1992) [12] recommends the use of the more simplified as only a preliminary analysis, if the other two methods are not used. For this reason, although the fatigue criterion of the NBR 6118 : 2003 [11] have been satisfied for the section in question, was additionally performed a more refined analysis according to Model Code MC90 (CEB-FIP, 1992) [12], and the results of this analysis are described below.

For the use of this more refined method, the actual Model Code MC90 (CEB-FIP, 1992) [12] suggest the use of algorithm Rain Flow for counting cycles. Using this algorithm can be carried out a

cycles counting of stresses in both the concrete and the reinforcement. From the cycle count obtained through the algorithm can be proceeded the fatigue analysis according to Model Code MC90 (CEB-FIP, 1992) [12]. Table 6 presents results from the fatigue analysis for section S21, considering the operational train type and Table 7 presents the results for the future train on the same section. The structural damage for each element (reinforcement and concrete) is determined independently and it is considered that the damage in the section is the largest damage of the structural elements individually. The lifetime is expressed in pairs of trains (loading blocks) and in years, considering the passage of 18 trains per day. It can be observed in the tables that the damage of the structural elements of the section is low, except for the concrete on the bottom surface of the section, which is very compressed. This concrete fiber is subject to high initial stresses due to the perma-



nent loading and is under great stress variations when the moving loads act. Because of this, the lifetime of the section is 1.33E +07 years approximately, for the operational train, and 7.05E +05 for the future train type.

Must be remarked that these lifetimes were estimated using the specified characteristic strength of concrete in the project (f_{ck} = 18 MPa). The other sections were also analyzed for fatigue and the results regarding lifetime are presented in Figure 29 (semi log scale), considering also the f_{ek} specified in the project for both operational and future trains. Figure 29 shows that occurs a reduction in the fatigue lifetime of the sections with the change of loading from operational to future train type. It is also observed that the lifetime of the sections located on the first support is very high (support at the abutment E1, section S1, x = 0 m) which did not occur in the third support sections (section S21, x = 40 m). In section S21 the critical element (suffering greater fatigue damage) is the concrete on the bottom surface. Therefore, based on the results obtained for other bridges already analyzed (bridges over the rivers Mearim, Cajuapara and Rio Vermelho), it is known that the real compressive strength of concrete is much higher than the value specified in the project. Thus, one must be considered the

Table 6 – Fatigue analysis for stringer's cross section S21 under operational train type loads							
Flowsork	Damage						
Element	Loaded train	Unloaded train	Total (pair)				
Bottom surface reinforcement	1.09 E-11	5.02 E-13	1.14 E-11				
Top surface reinforcement	1.45 E-12	6.46 E-14	1.51 E-12				
Bottom surface concrete	5.83 E-13	1.58 E-19	5.83 E-13				
Top surface concrete	0.00 E+00	0.00 E+00	0.00 E+00				
	Section maximum do	1.14 E-11					
	Section lifetime in pair of trains		8.77 E+10				
	Section lifetime in ye	1.33 E+07					

Table 7 – Fatigue	analysis for stri	nger's cross section	n S21 under futur	e train type loads

Flowerk	Damage			
Element	Loaded train	Loaded train	Loaded train	
Bottom surface reinforcement	9.26 E-11	5.02 E-13	9.31 E-11	
Top surface reinforcement	1.32 E-11	6.46 E-14	1.33 E-11	
Bottom surface concrete	2.16 E-10	1.58 E-19	2.16 E-10	
Top surface concrete	0.00 E+00	0.00 E+00	0.00 E+00	
	Section maximum do	2.16 E-10		
	Section lifetime in pa	4.63 E+09		
	Section lifetime in yea	7.05 E+05		



possibility of extending the fatigue lifetime considering the current value of concrete strength obtained from sclerometry and axial compression tests on concrete testimonies.

6. Conclusions

After tests performed "in situ", the taken concrete testimonies were tested in laboratory and the results revealed that the concrete compression strengths are much higher than those specified in the project (18 MPa). Thus, the concrete of the current structure has a degree of safety higher than that stipulated in the preparation of structural design. The difference between the values for elasticity modulus of concrete (referring to f_{ck} stipulated in the project and the result obtained in the tests) was also considered in the computational models to verify the bridge structure in relation to ultimate limit states and serviceability limit states.

Based on direct observation of the state of the minerals, in the investigation of the maintenance history, which directly reflects the degree of reliability and integrity of the structure and of the theoretical models, it is concluded that at no studied point occurred corrosion in the reinforcements nor CO_2 penetration into the concrete layer corresponding to the coating. This indicates unfavorable conditions for the advance of carbonation front provided by the environment, giving a high reliability to the test results of sclerometry which may be strongly affected by this phenomenon, once according to the ACI 228R-89 (1989) [13] a carbonated surface layer results in sclerometric indexes greater than those corresponding to the inner layers of the structural element.

The sclerometry tests also revealed that resistance values do not suffer large dispersions when comparing elements relatively distant along the structure, which reinforces the hypothesis concerning "uniformity" in the strength of concrete. The pacometry tests served to ensure compatibility between the existing and designed reinforcements, but it is recommended to repeat the procedure on a larger number of regions. The axial compression tests according to NBR 5739 : 1994 and modulus of elasticity under the light of NBR 8522 : 2003 converge with those obtained by sclerometry and codes' estimates, and the perceived differences are justified by the different natures of the tests. The recommended values for the strain corresponding to the maximum stress of concrete are also close to those observed experimentally. The characteristic curve of the concrete, although atypical point modulus of elasticity commensurate with analyzed codes' estimates, however it is recommended campaigns for removal of a greater number of concrete testimonies to increase the representation of the conclusions related to the constitution of the bridge as a whole.

Regarding the fatigue results it was observed that the damage in the elements of the cross section is low, except for the concrete of the bottom surface of the section, which is very compressed due to the concrete fibers are subject to considerable initial stresses (permanent loading) suffering large stress variations with the passage of the moving loads. For the future loaded train, it was observed that the element of greatest damage corresponded to the bottom surface reinforcement and concrete of the studied cross section. Because of this it is possible state that the OAE 50A shows no fatigue problems.

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